

An Automata Based Approach for Verification of Information Flow Properties

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Framework

Events. *V*isible, *C*onfidential, *N*either

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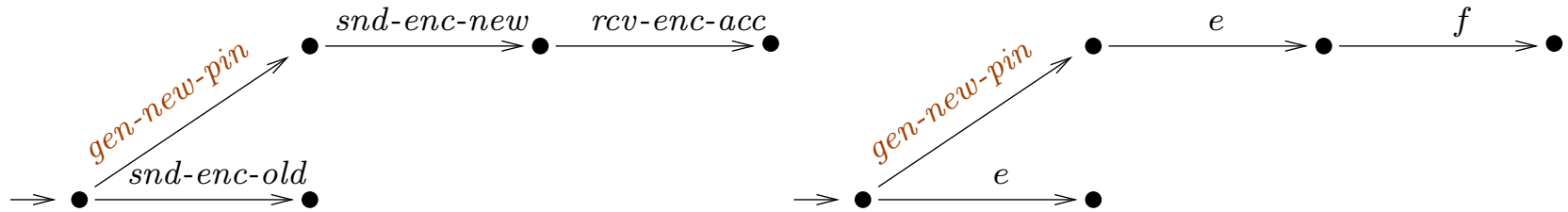
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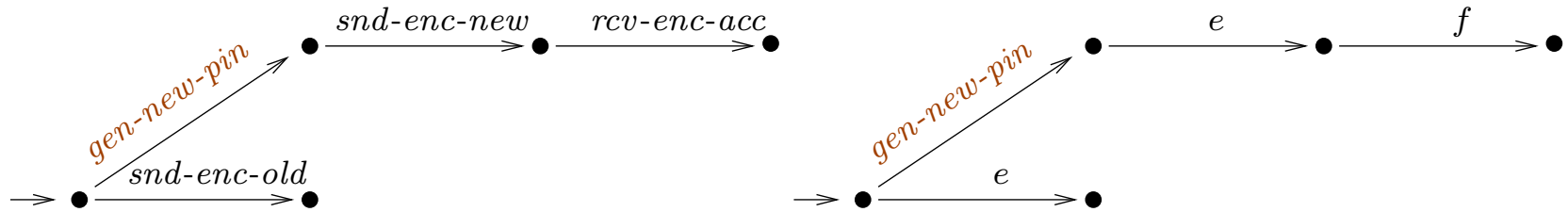
Non-Inference(*NF*)

$$\forall \tau \in L \Rightarrow \tau \upharpoonright_V \in L$$

An Example



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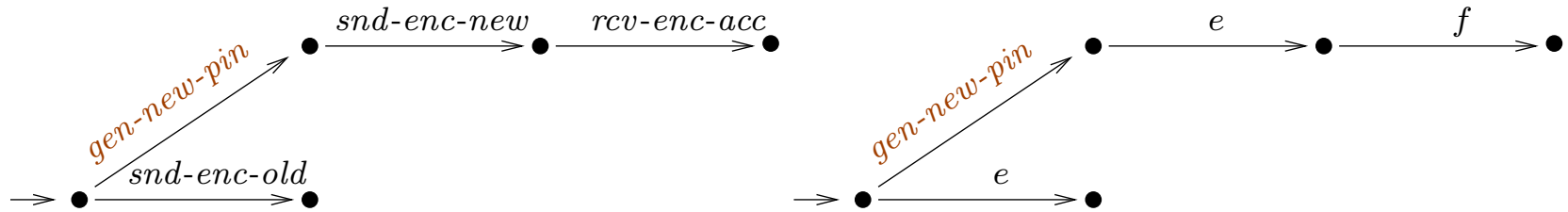


$$V = \{e, f\}$$

$$C = \{gen-new-pin\}$$

$$N = \phi$$

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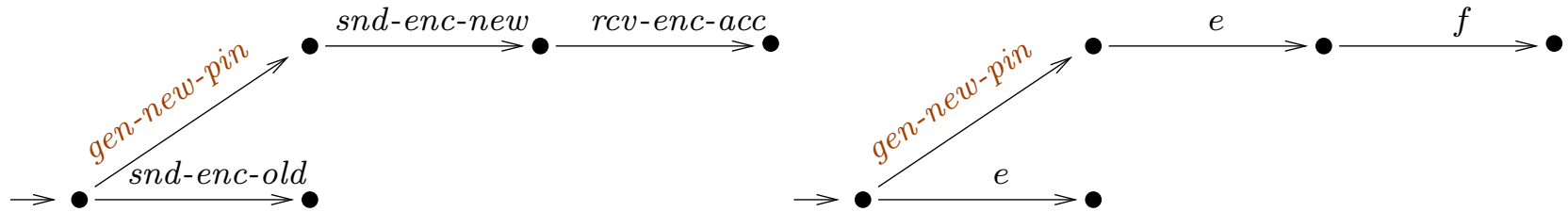
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$$Tr = \{ \text{gen-new-pin } e \ f, \\ e \} + \text{prefixes}$$

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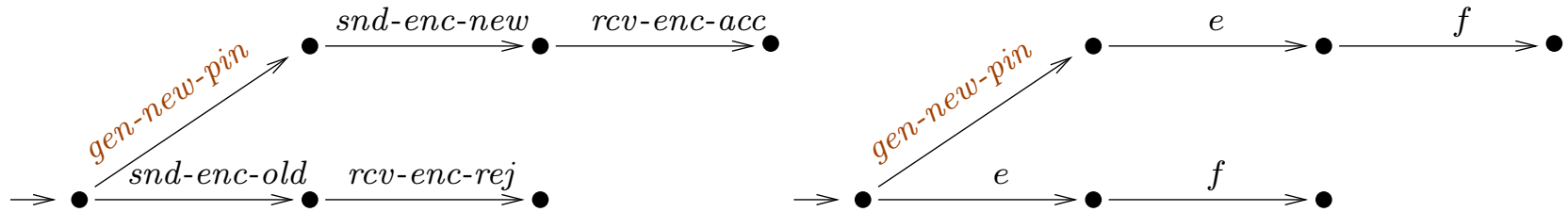
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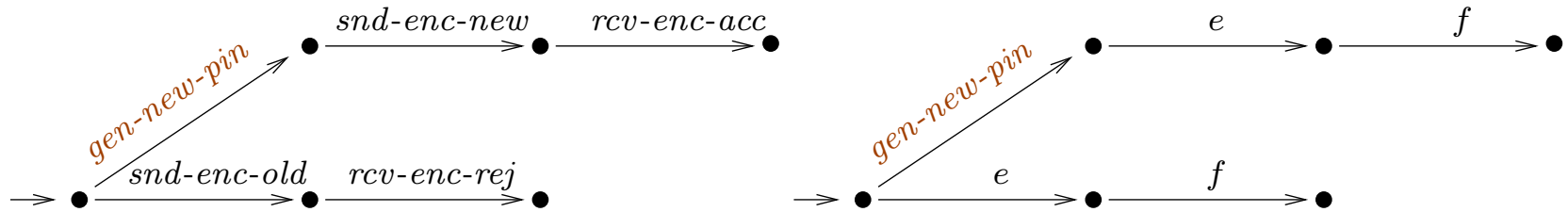
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Confidentiality compromised. Noninference fails

Example ...contd



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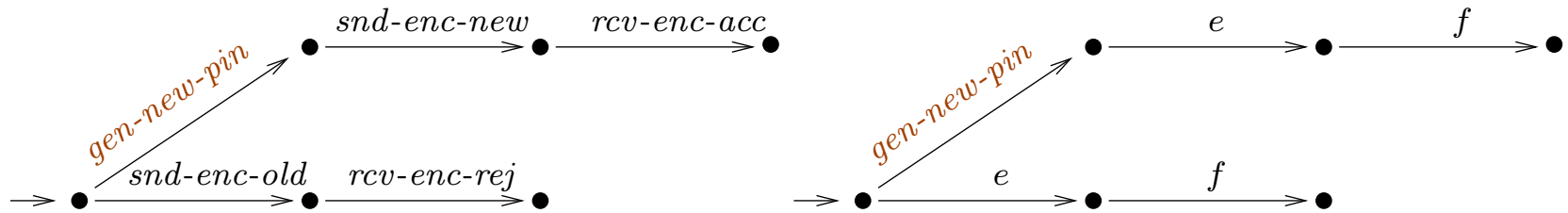


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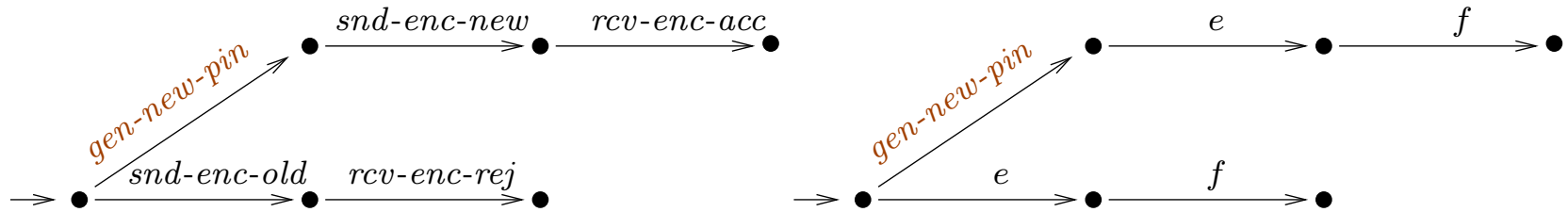
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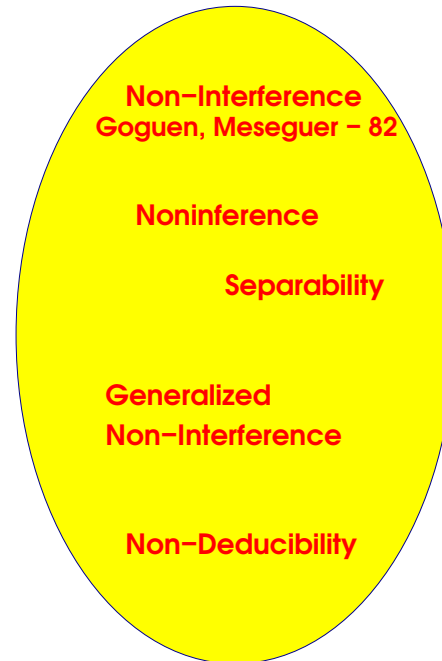
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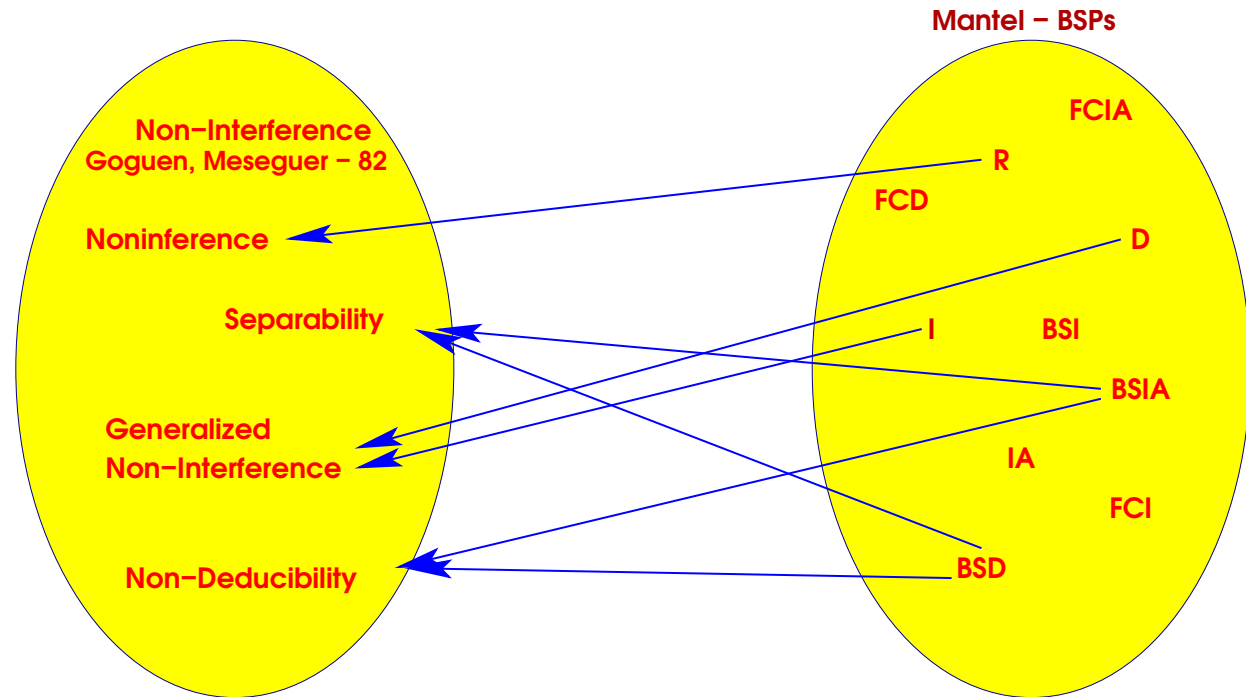
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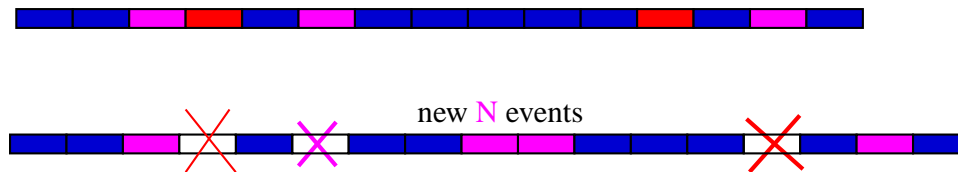
Basic Security Predicates (BSPs)

Trace based information flow properties in BSPs

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BSP Removal (R)



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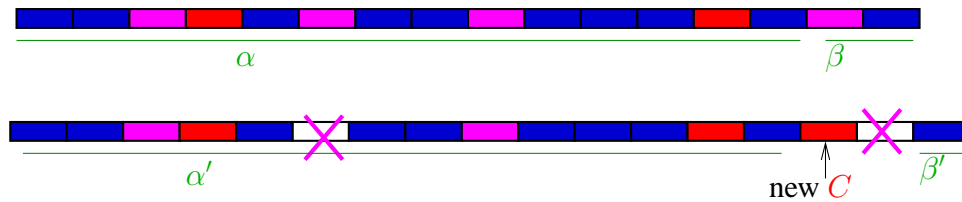
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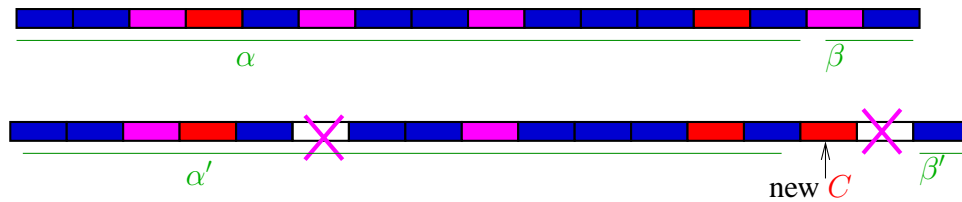
BSP Insertion (I)



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BSP Insert- X Admissable (IA)

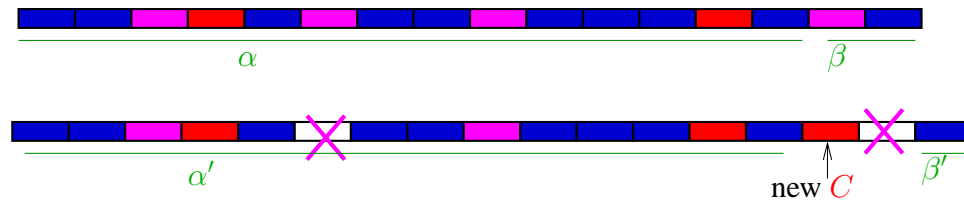


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Generalized Non-Interference - I and D

Noninference - R

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Model Check - BSP on Finite State Automaton

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- Removal R iff $L \upharpoonright_V \subseteq_N L$.
- Deletion D iff $I\text{-del}(L) \subseteq_N L$.
- Insertion I iff $I\text{-ins}(L) \subseteq_N L$.
- Strict Removal SR iff $L \upharpoonright_{\overline{C}} \subseteq L$.
- Strict Deletion SD iff $I\text{-del}(L) \subseteq L$.

Language Inclusion Problem for BSP D

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τ' equivalent to τ modulo N -corrections

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$$L \upharpoonright_X$$

by replacing transitions $p \xrightarrow{a} q$, with $a \notin X$, in \mathcal{A} , by an ϵ -transition $p \xrightarrow{\epsilon} q$

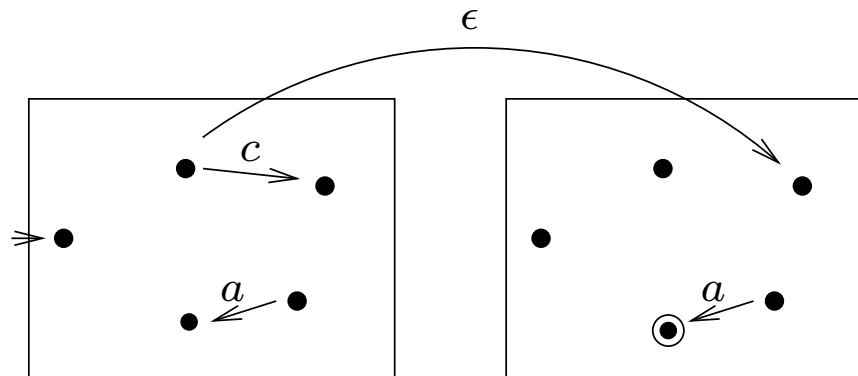
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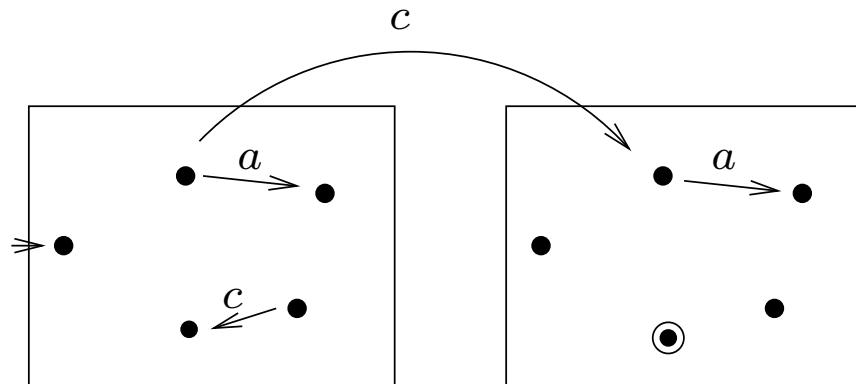
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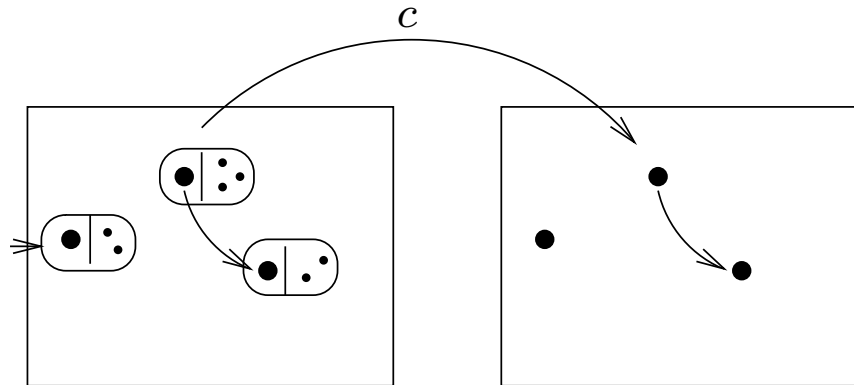
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BSPs - Special case of First Order Logic? Decidability?

Thank You